

Liquidity and Safety over the Business Cycle

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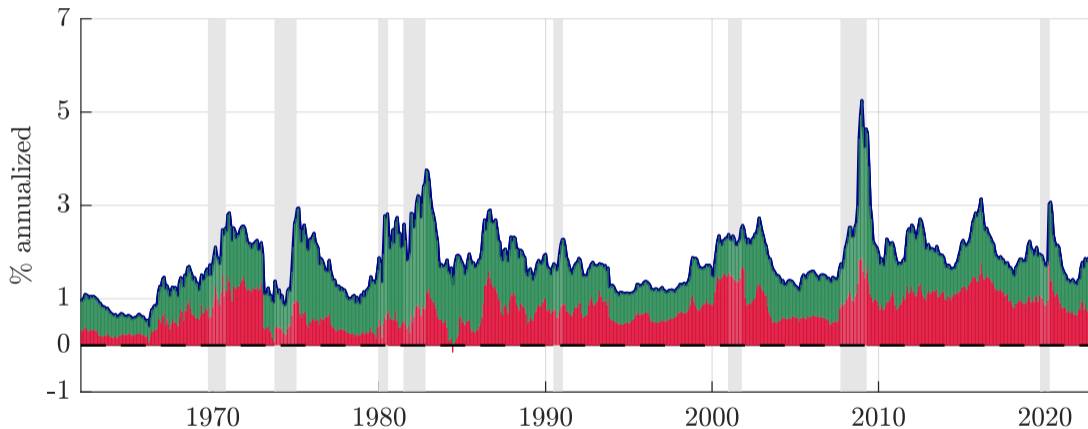
Motivation

- Broad consensus in macro-finance literature:
 - ▶ Financial conditions relevant over the business cycle
[Kiyotaki & Moore 1997; Bernanke, Gertler & Gilchrist 1999]
 - ▶ In particular, both erosion of safety & dry-up of liquidity associated with early stages of 2007/08 Great Financial Crisis
[Taylor & Williams 2009; Bernanke 2010, 2018; Gorton & Metrick 2010, 2012]
- **Liquidity and safety are broad (and interlinked) concepts**
 - ▶ Hard to separate but **distinction critical for policy design** in crises (credit easing in 07/08; March-2020) & **interlinked with fiscal multipliers**
 - ▶ Krishnamurthy & Vissing-Jorgensen (2012) suggest empirical decomposition
- This paper: **identify structural drivers of empirical liquidity & safety** in terms of shocks to supply of safe assets, asset resaleability & asset quality

Convenience yield



Convenience yield | Liquidity & Safety



This paper

- Endogenize both the liquidity & safety of private assets in a medium-scale NK model with heterogeneous firms and two financial frictions
 - ▶ **Liquidity:** resaleability constraint on private assets
 - ▶ **Safety:** shocks to asset quality & asymmetric information
- Estimate the model over the U.S. business cycle matching empirical liquidity and safety premia → highlight **role of two types of financial shocks**
- **Crisis simulations & policy counterfactuals** for Fin Crisis & March-2020 → policy implications (role of QE, fiscal multipliers), liquidity puzzle ...

Literature

- **Markets in the GFC** | Brunnermeier & Pedersen (2009); Taylor & Williams (2009); Ashcraft, Garleanu & Pederson (2010); Gorton & Metrick (2010, 2012) ...
- **Safe assets** | Krishnamurthy & Vissing-Jorgensen (2012); He, Krishnamurthy & Milbradt (2016, 2019); Caballero, Farhi & Gourinchas (2017); Caballero & Farhi (2018); Bayer, Born & Luetticke (2023) ...
- **Asset quality (& asymmetric information)** | Kurlat (2013); Bigio (2015); Dong & Wen (2023); Bierdel, Drenik, Herreño & Ottonello (2023) ...
- **Asset resaleability** | Kiyotaki & Moore [KM] (1997, 2019); Ajello (2016); Del Negro, Eggertsson, Ferrero & Kiyotaki [DEFK] (2017) ...
- **Business cycle fluctuations** | Justiniano, Primiceri & Tambalotti (2010); Christiano, Motto & Rostagno (2014); Becard & Gauthier (2021) ...
- **Liquidity puzzle** | Shi (2015); Guerron-Quintana & Jinnai (2019) ...

I. Motivation

II. Model

III. Estimation & Results

IV. Liquidity puzzle

V. Next steps

The model in a nutshell

- Households ▶ Households
 - ▶ Consume, supply labour & own firms and retailers
- Labour unions & investment goods firms ▶ Labour unions ▶ Investment goods firms
 - ▶ Differentiate homogeneous labour & set wages on a staggered basis
 - ▶ Transform final goods into investment goods
- **Heterogeneous firms (producers/ entrepreneurs)**
 - ▶ **Produce intermediate good**
 - ▶ **Invest in new capital formation & trade existing capital subject to**
 - idiosyncratic investment efficiency ϵ_t
 - the current resaleability ($\bar{\omega}_t$) and quality of capital ($\bar{\psi}_t$)
- Final goods firms & monetary and fiscal policy ▶ Final goods firms ▶ Government
 - ▶ Differentiate homogeneous intermediate good & set prices on a staggered basis
 - ▶ Interest rate policy, ZLB & government budget constraint

Heterogeneous firms: Production

Firms produce subject to a pre-determined capital stock, maximizing

$$R_{Kt}k_{it-1} \equiv P_{mt}a_t (u_{it}k_{it-1})^\alpha (z_t\ell_{it})^{1-\alpha} - W_t\ell_{it} - s(u_{it})k_{it-1}.$$

Given homogeneity of intermediate output, constant returns to scale, and the absence of idiosyncratic disturbances \rightarrow conventional aggregate relationships:

$$y_{mt} = a_t (u_t k_{t-1})^\alpha (z_t \ell_t)^{1-\alpha} \quad w_t = (1 - \alpha) \frac{p_{mt} y_{mt}}{\ell_t}$$

$$s'(u_t) = \alpha \frac{p_{mt} y_{mt}}{u_t k_{t-1}} \quad r_{Kt} k_{t-1} = \alpha p_{mt} y_{mt} - s(u_t) k_{t-1}$$

Heterogeneous firms: Investment

Firms invest in new capital formation & trade existing capital, maximizing

$$\mathbb{V}^P(k_{it-1}, b_{it-1}, \epsilon_t) \equiv \mathbb{V}_{it}^P = \mathbb{E}_t \left(\sum_{s=0}^{\infty} \mathcal{M}_{t+s} D_{it+s} \right)$$

subject to

$$D_{it} = R_{Kt} k_{it-1} - P_{It} i_{it} + P_{Kt} (k_{it}^{s,g} + k_{it}^{s,b} - k_{it}^a) + R_{t-1} B_{it-1} - B_{it}$$

$$k_{it} = (1 - \gamma) \bar{\psi}_t k_{it-1} + \psi_t^* k_{it}^a - k_{it}^{s,g} + \epsilon_t i_{it}$$

$$k_{it}^{s,g} \leq \bar{\omega}_t \bar{\psi}_t (1 - \gamma) k_{it-1} \quad \text{and} \quad k_{it}^{s,b} \leq \bar{\omega}_t (1 - \bar{\psi}_t) (1 - \gamma) k_{it-1}$$

$$\left\{ D_{it}, i_{it}, k_{it}, k_{it}^{s,g}, k_{it}^{s,b}, k_{it}^a, B_{it} \right\}_{t=0}^{\infty} \geq 0$$

In more detail | Three state variables

- Idiosyncratic investment efficiency $\epsilon_t \sim F(\epsilon_t)$
- Capital k_{it} : production factor & financial asset
→ subject to two financial frictions:
 - ▶ [ff 1] limited resaleability (liquidity) of capital $\bar{\omega}_t$
 - ▶ [ff 2] limited quality (safety) of capital $\bar{\psi}_t$ & asymmetric information
- Government bonds B_{it} : financial asset
→ supplied by the fiscal authority, perfectly liquid and safe

Heterogeneous firms: Investment

Firms invest in new capital formation & trade existing capital, maximizing

$$\mathbb{V}^P(k_{it-1}, b_{it-1}, \epsilon_t) \equiv \mathbb{V}_{it}^P = \mathbb{E}_t \left(\sum_{s=0}^{\infty} \mathcal{M}_{t+s} D_{it+s} \right)$$

subject to

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$$k_{it} = (1 - \gamma) \bar{\psi}_t k_{it-1} + \psi_t^* k_{it}^a - k_{it}^{s,g} + \epsilon_t i_{it}$$

$$k_{it}^{s,g} \leq \bar{\omega}_t \bar{\psi}_t (1 - \gamma) k_{it-1} \quad \text{and} \quad k_{it}^{s,b} \leq \bar{\omega}_t (1 - \bar{\psi}_t) (1 - \gamma) k_{it-1}$$

$$\left\{ D_{it}, i_{it}, k_{it}, k_{it}^{s,g}, k_{it}^{s,b}, k_{it}^a, B_{it} \right\}_{t=0}^{\infty} \geq 0$$

Heterogeneous firms: Investment

- Law of motion of capital: $k_{it} = (1 - \gamma) \bar{\psi}_t k_{it-1} + \epsilon_t i_{it} - k_{it}^{s,g} + \psi_t^* k_{it}^a$
- Resaleability constraints on good- and bad-quality capital:

$$k_{it}^{s,g} \leq \bar{\omega}_t \bar{\psi}_t (1 - \gamma) k_{it-1} \quad \text{and} \quad k_{it}^{s,b} \leq \bar{\omega}_t (1 - \bar{\psi}_t) (1 - \gamma) k_{it-1}$$

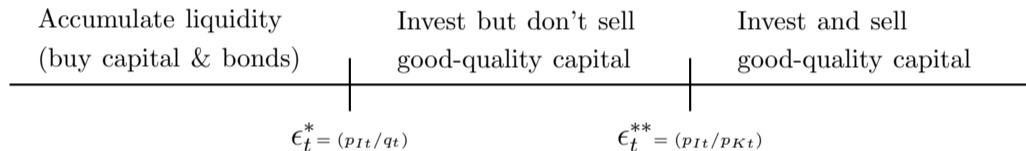
- Non-negativity constraints: $\left\{ D_{it}, i_{it}, k_{it}, k_{it}^{s,g}, k_{it}^{s,b}, k_{it}^a, B_{it} \right\}_{t=0}^{\infty} \geq 0$

Idiosyncratic investment efficiency $\epsilon_t \sim F(\epsilon_t)$

[ff 1] Resaleability of capital $\bar{\omega}_t$ **[ff 2]** Quality of capital $\bar{\psi}_t$ (w/ asym inf: ψ_t^*)

In more detail | Decision rules & aggregation

Realization of $\epsilon_t \sim F(\epsilon_t)$: Firms self-select into **three distinct groups**



Aggregation? (i) IID shocks; (ii) firm-behavior linear in state variables;
 (iii) cut-off values only depend on aggregate realizations. ✓
 [compare w/ BGG 1999, contrast w/ joint hh structure in Shi 2015 & DEFK 2017]

In more detail | Fin frictions & liquidity + safety premia

Fin frictions cause **spread (convenience yield)** betw govt bond & capital return

- **[ff 1]** Limited resaleability of capital $\bar{\omega}_t$
→ widens wedge between q_t and q_{Bt}
- **[ff 2]** Limited quality (safety) of capital $\bar{\psi}_t$ & asymmetric information
→ creates wedge between q_t and p_{Kt}

Nested models? With $\bar{\psi}_t = 1$ or no asymmetric information:

[ff 2] turned off, $q_t = p_{Kt}$ and $\epsilon_t^* = \epsilon_t^{**}$ [think KM 1997 or DEFK 2017]

Interior solutions? Endogenous adjustment to looser fin conditions via ϵ_t^* .
No need to (i) compute a separate unconstrained (interior) model solution [vs DEFK 2017], (ii) model frictions as occ binding constraints (if $B_t < \bar{\bar{B}}_t$).

In more detail | Fin frictions & liquidity + safety premia

$$cy_t \equiv \mathbb{E}_t \left\{ \beta \frac{\lambda_{t+1}}{\lambda_t} \left[1 + \int_{\epsilon_{t+1}^*}^{\epsilon_{t+1}} \left(\frac{\epsilon_{t+1}}{\epsilon_{t+1}^*} - 1 \right) dF(\epsilon) \right] \left(r_{Kt+1}^* - \frac{R_t}{\Pi_{t+1}} \right) \right\} = r_t^\omega + r_t^\psi$$

$$\text{where } r_t^\omega \equiv \mathbb{E}_t \left\{ \beta \frac{\lambda_{t+1}}{\lambda_t} \left[\int_{\epsilon_{t+1}^*}^{\epsilon_{t+1}^{\max}} \left(\frac{\epsilon_{t+1}}{\epsilon_{t+1}^*} - 1 \right) dF(\epsilon) \right] \frac{(1 - \bar{\omega}_{t+1})(1 - \delta_{t+1})q_{t+1}}{q_t} \right\},$$

$$r_t^\psi \equiv \mathbb{E}_t \left\{ \beta \frac{\lambda_{t+1}}{\lambda_t} \left[\int_{\epsilon_{t+1}^*}^{\epsilon_{t+1}^{\max}} \left(\frac{\epsilon_{t+1}}{\epsilon_{t+1}^*} - 1 \right) dF(\epsilon) - \int_{\epsilon_{t+1}^{**}}^{\epsilon_{t+1}^{\max}} \left(\frac{\epsilon_{t+1}}{\epsilon_{t+1}^{**}} - 1 \right) dF(\epsilon) \right] \frac{\bar{\omega}_{t+1}(1 - \delta_{t+1})q_{t+1}}{q_t} \right\} \\ - \mathbb{E}_t \left\{ \beta \frac{\lambda_{t+1}}{\lambda_t} \left[1 + \int_{\epsilon_{t+1}^*}^{\epsilon_{t+1}^{\max}} \left(\frac{\epsilon_{t+1}}{\epsilon_{t+1}^*} - 1 \right) dF(\epsilon) \right] \frac{\bar{\omega}_{t+1}(1 - \bar{\psi}_{t+1})(1 - \gamma)p_{Kt+1}}{q_t} \right\}$$

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The estimation in a nutshell

- **Model estimated using Bayesian methods** (parameter subset calibrated)
- Quarterly observations on 9 U.S. macro & financial variables from 1986–2019
 - ▶ 7 standard macro variables: GDP, consumption, investment, inflation, real wage, hours worked, fed funds rate (all quantities in real per capita terms)
 - ▶ 2 additional financial variables: **Liquidity and safety premia**
[Extensions: Price of investment goods and public debt/GDP ratio]
- Model stationarized and with 10 exogenous shock processes
- Data transformations: First-differences of trending variables, all demeaned

Calibrated parameters

Parameter		Value	Parameter		Value
Households					
σ	Risk aversion	1.0000	β	Discount factor	0.9901
χ	Disutility weight on labor	0.8011	ξ	Curvature of labor disutility	1.0000
Labor unions			Investment goods firms		
θ_p	Elasticity of labor substitution	11.000	Υ	Trend in inv specific technology	1.0025
Producers					
α	Capital share	0.4000	γ	Depreciation rate	0.0216
ν	Inv efficiency: Pareto param	5.7661	ε_{\min}	Inv efficiency: Pareto bound	0.8266
a	Steady state cyclical productivity	1.0000	μ_{z^*}	Trend growth rate of economy	1.0038
$\bar{\omega}$	Steady state capital resaleability	0.7740	$\bar{\psi}$	Steady state capital quality	0.9966
Final goods firms			Government		
θ_w	Elasticity of goods substitution	6.0000	Π^*	Steady state inflation	1.0050
g/y	Steady state govt spending/GDP	0.2000	b/y	Steady state govt debt/GDP	1.6772

NOTE: All parameters are either calibrated to match standard targets in the literature or mean values of observables. In particular, $\bar{\omega}$ and $\bar{\psi}$ are calibrated to match the average safety and liquidity premia in the sample.

Estimated parameters I

Parameter	Distr	Prior		Posterior		
		Mean	SD	Mode	SD	
(A) Economic parameters						
Households						
h	Habit parameter	beta	0.5000	0.1500	0.6589	0.0544
Labor unions						
ι_w	Calvo wage stickiness	beta	0.7500	0.1500	0.4423	0.0643
γ_w	Wage indexing weight on π_{t-1}	beta	0.5000	0.1500	0.6298	0.1553
Investment goods firms						
f''	Curvature of inv adj costs	normal	5.0000	3.0000	1.0333	0.1506
Producers						
σ_s	Curvature of cap util costs	normal	1.0000	1.0000	5.1870	0.6348
Final goods firms						
ι_p	Calvo price stickiness	beta	0.7500	0.1500	0.7975	0.0235
γ_p	Price indexing weight on π_{t-1}	beta	0.5000	0.1500	0.1256	0.0531
Government						
ϕ_π	Policy weight on inflation	gamma	1.5000	0.2500	2.6894	0.2337
ϕ_y	Policy weight on output	gamma	0.2500	0.1000	0.1442	0.0557
ρ_m	Policy inertia parameter	beta	0.8000	0.1000	0.8383	0.0161

Estimated parameters II

Parameter	Prior			Posterior		
	Distr	Mean	SD	Mode	SD	
(B) Exogenous processes						
$\rho_{\chi w}$	AC wage mark-up shock	beta	0.5000	0.2000	0.9839	0.0117
$\sigma_{\chi w}$	SD wage mark-up innovation	invg2	0.0100	1.0000	0.0235	0.0035
ρ_a	AC cyclical productivity shock	beta	0.5000	0.2000	0.2089	0.1519
σ_a	SD cyclical productivity innovation	invg2	0.0100	1.0000	0.0020	0.0004
ρ_z	AC trend growth rate shock	beta	0.5000	0.2000	0.3781	0.1279
σ_z	SD trend growth rate innovation	invg2	0.0100	1.0000	0.0060	0.0009
ρ_{ψ}	AC capital quality shock	beta	0.5000	0.2000	0.8938	0.0316
σ_{ψ}	SD capital quality innovation	invg2	0.0100	1.0000	0.0023	0.0002
ρ_{ω}	AC capital resaleability shock	beta	0.5000	0.2000	0.7996	0.0426
σ_{ω}	SD capital resaleability innovation	invg2	0.0100	1.0000	0.0647	0.0052
$\rho_{\chi p}$	AC price mark-up shock	beta	0.5000	0.2000	0.8997	0.0379
$\sigma_{\chi p}$	SD price mark-up innovation	invg2	0.0100	1.0000	0.0188	0.0032
σ_m	SD monetary policy innovation	invg2	0.0100	1.0000	0.0013	0.0001
ρ_g	AC govt spending/GDP shock	beta	0.5000	0.2000	0.9674	0.0142
σ_g	SD govt spending/GDP innovation	invg2	0.0100	1.0000	0.0156	0.0009
ρ_b	AC govt debt/GDP shock	beta	0.5000	0.2000	0.7605	0.0283
σ_b	SD govt debt/GDP innovation	invg2	0.0100	1.0000	0.5050	0.0320
ρ_{β}	AC preference shock	beta	0.5000	0.2000	0.9496	0.0215
σ_{β}	SD preference innovation	invg2	0.0100	1.0000	0.0010	0.0004

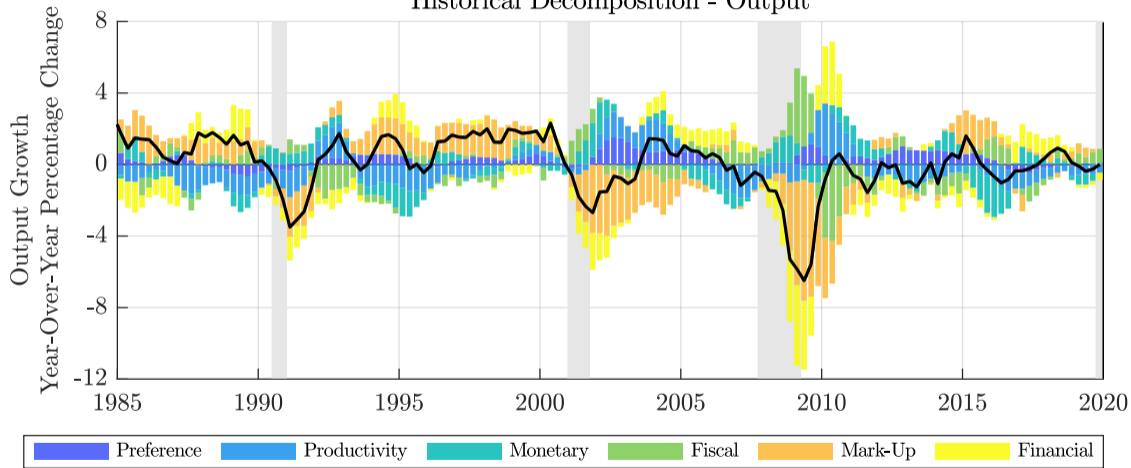
	$\varepsilon_{\chi wt}$	ε_{at}	ε_{zt}	$\varepsilon_{\psi t}$	$\varepsilon_{\omega t}$	$\varepsilon_{\chi pt}$	ε_{mt}	ε_{gt}	ε_{bt}	$\varepsilon_{\beta t}$
y_t	27.26	0.03	8.13	13.53	0.48	33.93	4.74	4.23	2.56	5.11
i_t	11.85	0.01	0.86	24.08	0.57	25.45	2.30	0.34	3.72	30.83
c_t	11.41	0.00	30.43	7.51	0.11	0.95	0.58	3.62	0.68	44.71
Π_t	5.43	0.73	2.00	35.66	1.04	15.77	21.46	1.29	6.43	10.19
R_t	2.16	0.05	1.29	59.11	1.39	4.62	13.37	1.07	10.41	6.53
cy_t	0.29	0.00	0.13	51.55	7.30	0.66	0.06	0.02	39.00	0.99
r_t^ψ	0.40	0.00	0.18	34.93	7.40	0.87	0.07	0.03	54.71	1.40
r_t^ω	0.02	0.00	0.01	5.36	90.71	0.04	0.00	0.00	3.75	0.10

NOTE: This table displays the percent of the variance of the endogenous variables (rows) explained by the structural shocks in the model (columns) at business cycle frequency (HP-filtered variables with $\lambda = 1600$).

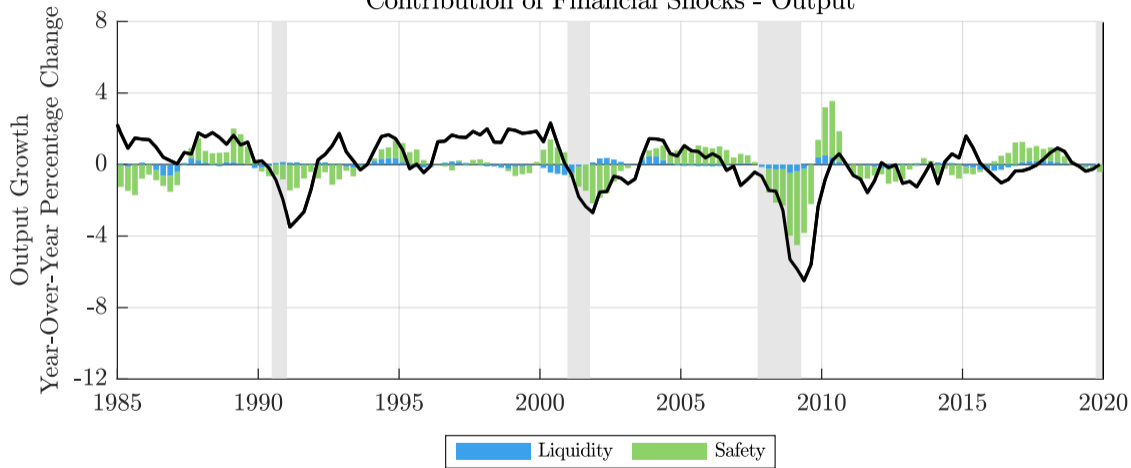
Preliminary results: Overview

- Unconditional variance decomposition of estimated model shows **important role for financial shocks** over the business cycle
- **Shocks to asset quality** ($\epsilon_{\psi t}$) [safety] are key, more so than shocks to asset resaleability ($\epsilon_{\omega t}$) [liquidity]
- **Shocks to supply of save assets** (ϵ_{bt}) relevant for spreads, but less important in explaining variation in real variables
- **Historical decomposition (next) confirms this** for key macro and financial variables over the sample from 1986 to 2019

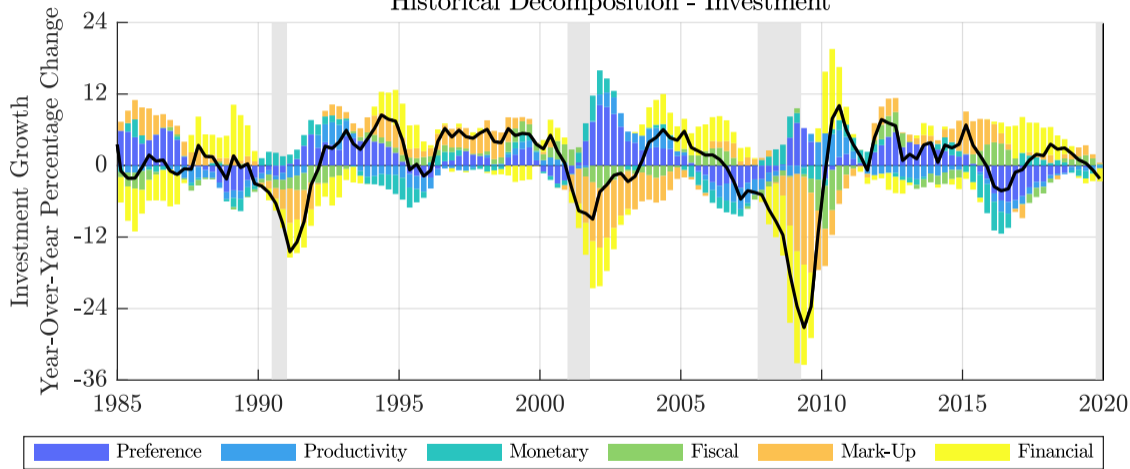
Historical Decomposition - Output



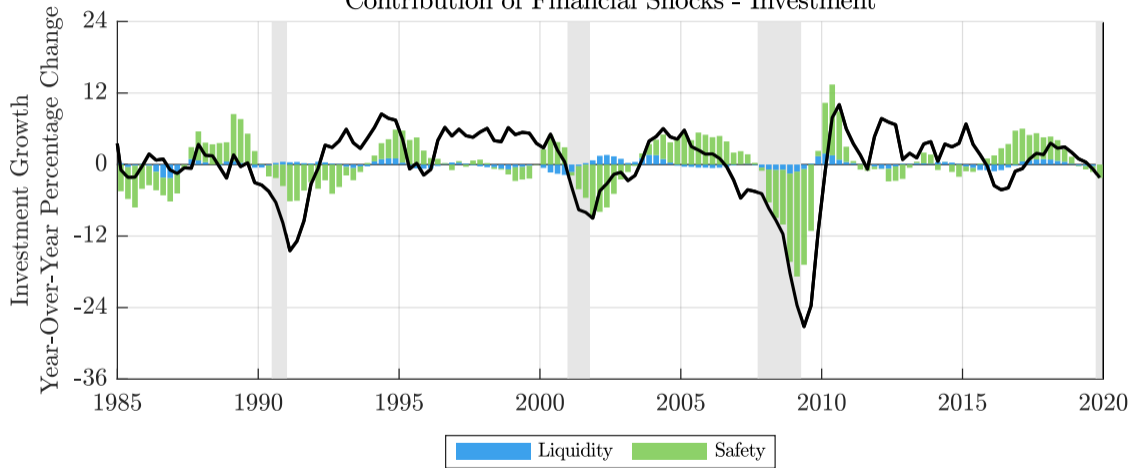
Contribution of Financial Shocks - Output

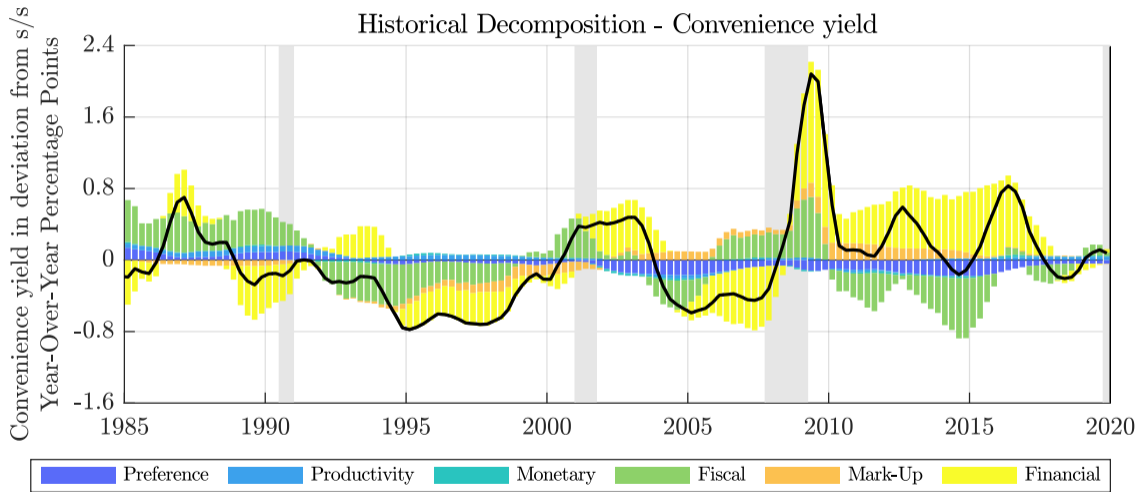


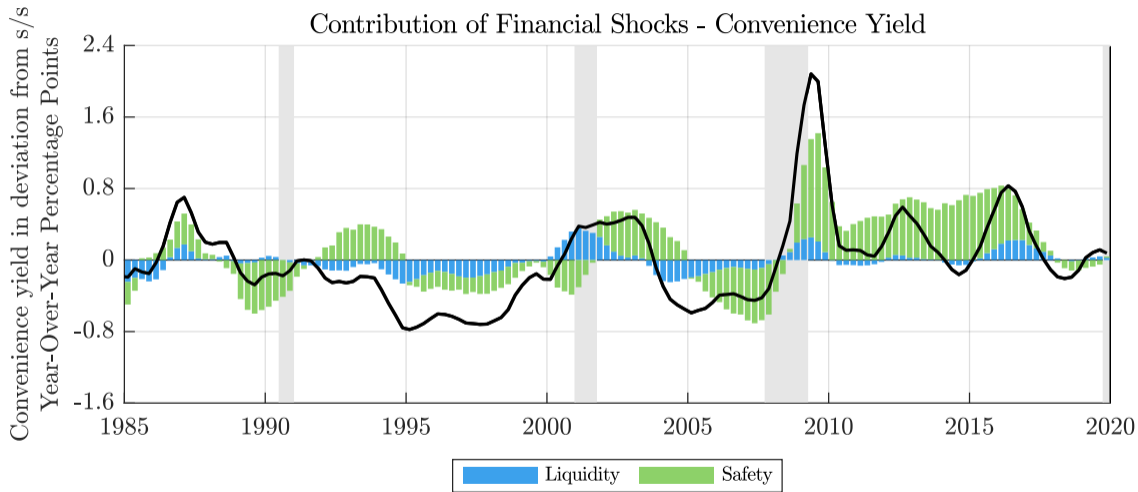
Historical Decomposition - Investment

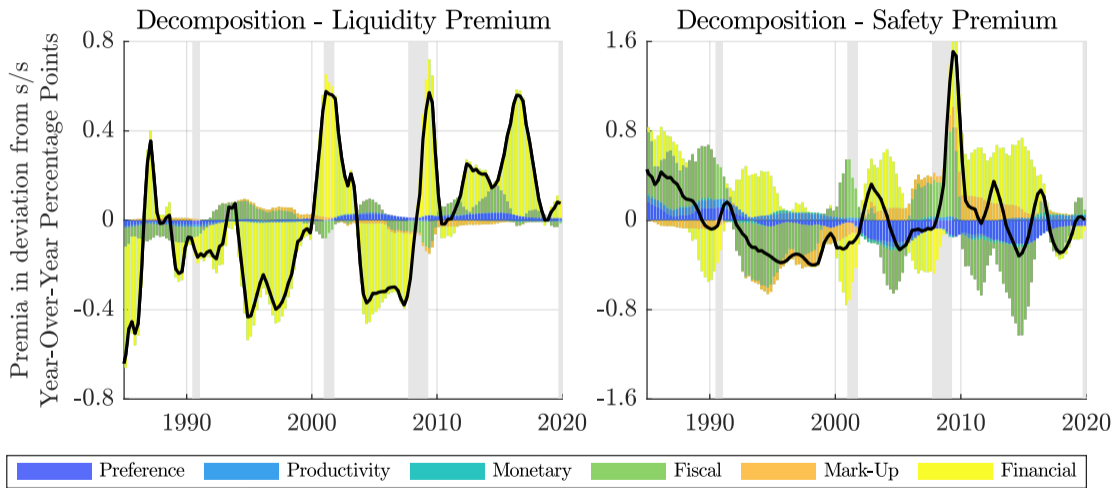


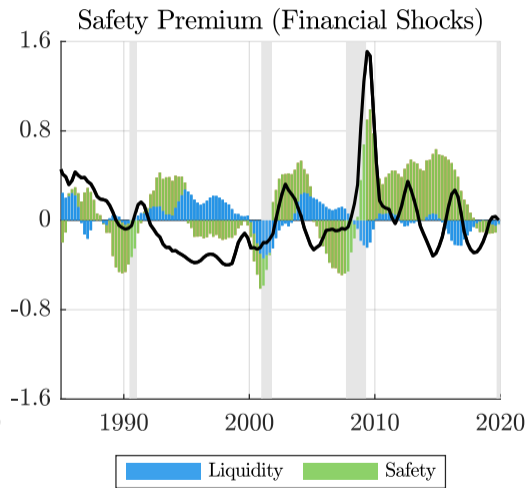
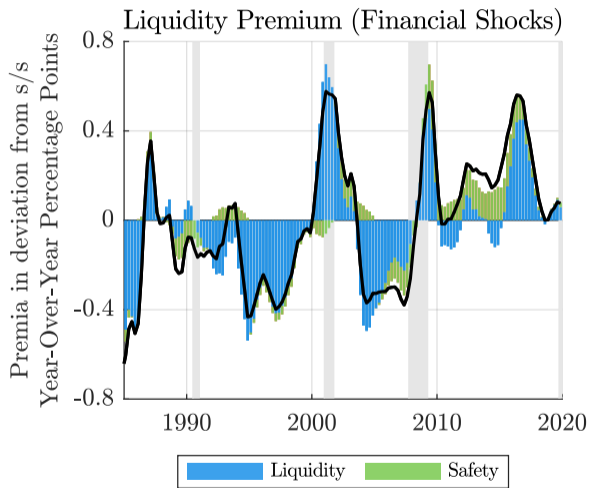
Contribution of Financial Shocks - Investment











I. Motivation

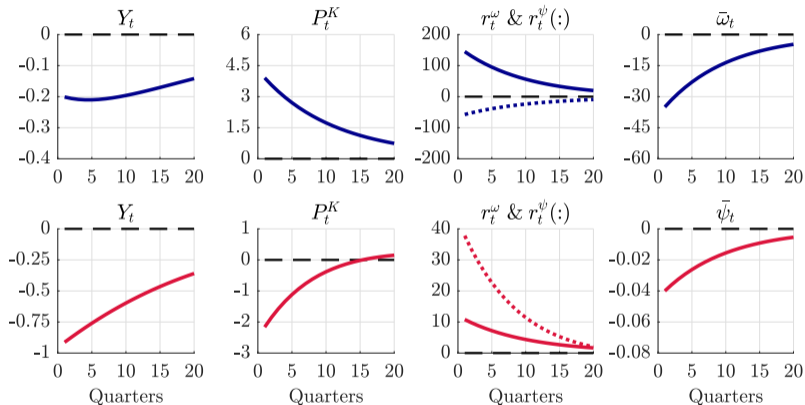
II. Model

III. Estimation & Results

IV. Liquidity puzzle

V. Next steps

In more detail | A model without nominal rigidities



Note: Row 1 (blue) gives impulse responses for a shock to capital resaleability (liquidity), row 2 (red) displays impulse responses for a shock to capital quality (safety). Y_t is output, P_t^K is the price of capital, r_t^ω and r_t^ψ are liquidity and safety premia, respectively. \bar{w}_t , which is capital resaleability, and $\bar{\psi}_t$, which is the fraction of high-quality assets, display the respective exogenous disturbances. All impulse responses are given in % deviations from steady state.

The liquidity puzzle

Counterfactual asset price response: Models with a liquidity friction à la KM (2019) predict a stock market boom following an adverse financial shock.

- Shi (2015): Robust result; need a fall in the perceived quality of capital
- Ajello (2016): Nominal + real rigidities & shock to intermediation
- Guerron-Quintana and Jinnai (2019): Endogenous growth \rightarrow LR dividends \downarrow
- Kiyotaki and Moore (2019): Storage technology & CB liquidity injection

This paper: **Nominal rigidities & ZLB** (in the spirit of DEFK 2017)

In more detail | Intuition

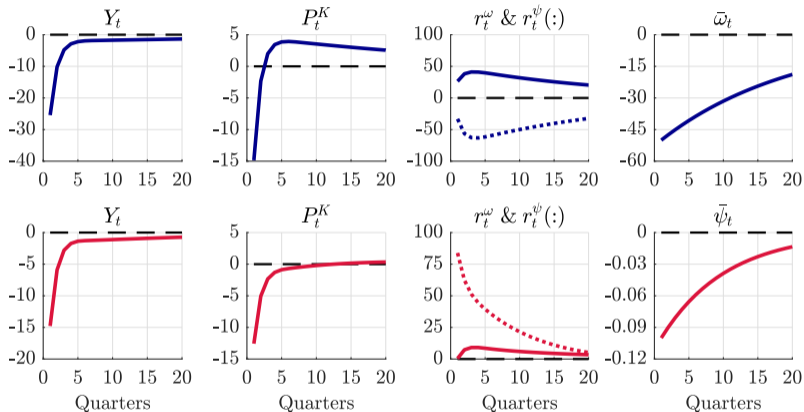
- At ZLB, $R_t = 1$ & $\mathbb{E}_t r_{t+1} \equiv (R_t / \mathbb{E}_t \Pi_{t+1}) \uparrow$. Via arbitrage, $\mathbb{E}_t r_{Kt+1}^* \uparrow$.

$$\mathbb{E}_t r_{Kt+1}^* \uparrow \equiv \frac{\mathbb{E}_t r_{Kt+1} + (1 - \gamma) \mathbb{E}_t \bar{\psi}_{t+1} q_{t+1} \uparrow}{q_t \downarrow}$$

Note, however,

- $\mathbb{E}_t r_{Kt+1}^* - \mathbb{E}_t r_{t+1} \neq \text{constant}$ (but $\bar{\omega}_t \downarrow \rightarrow cy_t \uparrow$)
- $\mathbb{E}_t r_{Kt+1} \neq \text{constant}$ (but slow-moving K_t and a_t pro-cyclical)
- $q_t \neq p_{Kt}$ (but $p_{Kt} = \psi_t^* q_t$)

In more detail | A model with nominal rigidities & ZLB



Note: Row 1 (blue) gives impulse responses for a shock to capital resaleability (liquidity), row 2 (red) displays impulse responses for a shock to capital quality (safety). Y_t is output, P_t^K is the price of capital, r_t^ω and r_t^ψ are liquidity and safety premia, respectively. $\bar{\omega}_t$ - capital resaleability - and $\bar{\psi}_t$ - the fraction of high-quality assets - are the respective exogenous disturbances, **set to bring the model to the ZLB for 4 periods**. All impulse responses are given in % deviations from steady state. [► Calibration](#)

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This version

- Motivation [liquidity and safety over the business cycle]
- Model [medium-scale NK model w/ two financial frictions; insights]
- Estimation [data; historical decomposition; role of financial shocks]
- Liquidity puzzle [Nominal rigidities & ZLB]

Work in progress

- Estimation
 - ▶ data on public liquidity
- Crisis simulations & policy counterfactuals
 - ▶ impulse responses, forecast-errors, liquidity puzzle at ZLB
 - ▶ role of CB liquidity provision; March-2020 liquidity crunch; fiscal multipliers

Extra slides

Model: Households

- Consume, supply labor & own firms and retailers

The representative household maximizes

$$\mathbb{V}_t^H = \mathbb{E}_t \left\{ \sum_{s=0}^{\infty} \beta^s \left[\ln(c_{t+s} - \bar{h}c_{t+s-1}) - \frac{\chi}{1+\xi} \ell_{ht+s}^{1+\xi} \right] \right\}$$

subject to

$$P_t c_t + \int_{i \in [0,1]} V_{it} s_{it} di = W_{ht} \ell_{ht} + \int_{i \in [0,1]} (V_{it} + D_{it}) s_{it-1} di + \Omega_t - T_t,$$

◀ main part

Model: Labor unions

► Differentiate homogeneous labour & set wages on a staggered basis

$$\max_{\widetilde{W}_{lt}} \mathbb{E}_t \left\{ \sum_{s=0}^{\infty} \iota_w^s \mathcal{M}_{t+s} \left[(1 - \tau_{wt+s}) \widetilde{W}_{lt} X_{t,t+s}^W - W_{ht+s} \right] \ell_{lt,t+s} \right\}$$

subject to

$$\ell_{lt,t+s} = \left(\frac{\widetilde{W}_{lt} X_{t,t+s}^W}{W_{t+s}} \right)^{-\theta_w} \ell_{t+s},$$

$$X_{t,t+s}^W = \begin{cases} \prod_{k=0}^{s-1} (\mu_{zt+k+1})^{\gamma_\mu} (\mu_z)^{1-\gamma_\mu} (\Pi_{t+k})^{\gamma_w} (\Pi_{t+k+1}^*)^{1-\gamma_w} & \text{if } s > 0 \\ 1 & \text{if } s = 0 \end{cases}$$

◀ main part

Model: Investment goods firms

- Transform final goods into investment goods

The representative investment goods firm maximizes

$$\mathbb{V}_t^I = \mathbb{E}_t \left\{ \sum_{s=0}^{\infty} \mathcal{M}_{t+s} \left\{ P_{It+s} - \left[1 + f \left(\frac{i_{t+s}}{i_{t+s-1}} \right) \right] P_{t+s} \right\} i_{t+s} \right\}$$

where

$$f(x_t) \equiv \frac{1}{2} \left\{ \exp \left[\sqrt{f''} (x_t - x) \right] + \exp \left[-\sqrt{f''} (x_t - x) \right] - 2 \right\}$$

◀ main part

Model: Final goods firms

► Differentiate homogeneous goods & set prices on a staggered basis

$$\max_{\tilde{P}_{jt}} \mathbb{E}_t \left\{ \sum_{s=0}^{\infty} \iota_p^s \mathcal{M}_{t+s} \left[(1 - \tau_{pt+s}) \tilde{P}_{jt} X_{t,t+s}^P - P_{mt+s} \right] y_{jt,t+s} \right\}$$

subject to

$$y_{jt,t+s} = \left(\frac{\tilde{P}_{jt} X_{t,t+s}^P}{P_{t+s}} \right)^{-\theta_p} y_{t+s},$$

$$X_{t,t+s}^P = \begin{cases} \prod_{k=0}^{s-1} (\Pi_{t+k})^{\gamma_p} (\Pi_{t+k+1}^*)^{1-\gamma_p} & \text{if } s > 0 \\ 1 & \text{if } s = 0 \end{cases}$$

◀ main part

Model: Monetary & fiscal policy

Interest rate policy, ZLB & government budget constraint

Monetary policy follows a standard Taylor Rule subject to the ZLB,

$$R_t = \max \left\{ R_{t-1}^{\rho_m} \left[R \left(\frac{\Pi_t}{\Pi_t^*} \right)^{\phi_\pi} \left(\frac{y_t/y_{t-1}}{\exp(\Gamma)} \right)^{\phi_y} \right]^{1-\rho_m} e^{\varepsilon_{mt}}, 1 \right\}$$

Govt spending & debt issuance are exogenous, the budget constraint is given by

$$B_{t+1} = R_t B_t + P_t g_t - T_t$$

[← main part](#)

Liquidity puzzle: Calibration of the simple model

[◀ main part](#)

Parameter		Value	Parameter		Value
Households					
σ	Risk aversion	1.000	β	Discount factor	0.985
\bar{h}	Habit parameter	0.815	χ	Utility weight on labor	6.420
ξ	Inverse Frisch elasticity	0.500			
Producers					
α	Capital share	0.360	γ	Depreciation rate	0.022
ν	Inv efficiency: Pareto param	7.140	ϵ_{\min}	Inv efficiency: Pareto bound	0.860
$\bar{\omega}$	SS capital resaleability (ff#1)	0.410	ψ	SS capital quality (ff#2)	0.997
Retailers					
ζ	Elasticity of substitution	11.00	ι	Probability of fixed prices	0.750
Government					
ϕ_{Π}	Policy rule inflation response	1.500	ϕ_X	Policy rule output response	0.125
ρ	Policy rule inertia	0.000	G/Y	SS Govt expenditure/ GDP	0.200
B/Y	SS Govt debt/ GDP	0.560			